| KS1   | Pupils should memorise and reason with numbers in 2, 5 and 10 times tables.<br>They should see ways to represent odd and even numbers and know how they are represented in tables. This will help them to understand the pattern in numbers.<br>Pupils should begin to understand multiplication as scaling in terms of double and half (e.g. that tower of cubes is double the height of the other tower).<br>Commutative law shown on array.<br>Repeated addition can be shown mentally on a number line.<br>Inverse relationship between multiplication and division. Use an array to explore how numbers can be organised into groups. |   |  |  |  |
|---|--|---|--|--|--|
| Year  | 3  | 4   |  |  |  |
| Layers of<br>vocabulary<br><b>Appendix 1a</b><br>Beck's Tiers<br>of<br>Vocabulary<br><b>Appendix</b><br><b>1b</b> :<br>Vocabulary<br>book | <ul> <li>Basic to subject specific (Beck's Tiers):</li> <li>lots of, groups of ×, times, multiply, multiplication, multiplied by multiple of, product once, twice, three times ten times times as (big, long, wide and so on) repeated addition array row, column double, halve share, share equally one each, two each, three each</li> <li>Instructional vocabulary:</li> <li>carry on, continue repeat what comes next? predict describe the pattern, describe the rule</li> <li>find, find all, find different, investigate</li> <li>choose, decide, collect</li> </ul>  | <ul> <li>Basic to subject specific (Beck's Tiers):</li> <li>lots of, groups of times, multiply, multiplication, multiplied by multiple of, product once, twice, three times ten times times as (big, long, wide and so on)</li> <li>repeated addition array row, column double, halve, factor, multiple</li> <li>Instructional vocabulary:</li> <li>carry on, continue, repeat what comes next? predict describe the pattern, describe the rule</li> <li>pattern, puzzle, calculate, calculation, mental calculation, method, jotting, answer right, correct, wrong what could we try next? how did you work it out? number sentence sign, operation, symbol, equation</li> </ul> |  |  |  |
| NC 2014   | Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including 2 digit numbers times 1 digit numbers progressing to formal written methods.   | Multiply 2 digit and 3 digit numbers by a 1 digit number using formal written layout. Solve problems involving multiplying and adding.  |  |  |  |

| Developing<br>Conceptual/<br>Procedural<br>Understanding | <b>Building tables</b><br>For example, build tables<br>using counting stick-<br>forwards and backwards<br>and with missing jumps<br><b>Using known facts</b><br>If 3 x 2 = 6, then 30 x 2 =<br>60, 60 ÷ 3 = 20 and<br>30 = 60 ÷ 2. | Partitioning strategy to<br>double<br>Double 35<br>$3022 \xrightarrow{5}{90} 5x^2$<br>Place value materials to<br>represent calculations<br>Partitioned numbers<br>15 x 5 = 75<br>10 x 5 = 50<br>5 x 5 = 25<br>27 x 3 = 81<br>20x3 = 60<br>7x3 = 21<br>"20 multiplied by 3 equals<br>60 and 7 multiplied by 3<br>equals 21. 60 add 21<br>equals 81." | Grid method $23 \times 8 =$ $20 \times 8 = 160$ $3 \times 8 = 24$ $23 \times 8 =$ $23 \times 8 =$ $23 \times 8 =$ $8$ $3 \times 8 =$ $24 \times 20$ $3 \times 8$ $24 \times 8$ $24 \times 8$ $160 \times 20$ $184$ leading to compact $23 \times 8$ $24 \times 8$ $160 \times 20$ $184$ leading to compact $23 \times 8$ $184$ $2$ RepresentingproblemsA group of aliens liveon Planet Xert.Tinions have threelegs, Quinions havefour legs. The grouphas 22 legsaltogether. Howmany Tinions andQuinions might therebe? Is there morethan one solution? | Building tablesFor example, build tablesusing counting stick-<br>forwards and backwards and<br>with missing jumpsUsing known factsIf $2 \times 3 = 6$ then $200 \times 3 = 600$<br>and $600 \div 3 = 200$ Distributivity<br>$3 \times (2 + 4) = 3 \times 2 + 3 \times 4$<br>So the '3' can be 'distributed'<br>across the '2 + 4' into 3 times<br>$2$ and 3 times 4Image: the logic | Place value materials to<br>represent calculations<br>Grid method<br>(if needed for conceptual<br>understanding)<br>$346 \times 9$<br>$\boxed{x 300 40 6}{9}$<br>Short multiplication<br>Expanded<br>346<br>$\xrightarrow{x 9}{54 (9 \times 6)}{360 (9 \times 40)}{2700 (9 \times 300)}{3114}$<br>leading to compact<br>346<br>$\xrightarrow{x 9}{3114}$<br>$_{4 5}$ | Representing problemsMultiply a number by itself and then<br>make one factor one more and the<br>other one less. What do you notice?<br>Does this always happen?Eg 4 x 4 = 16 $6 x 6 = 36$<br>$5 x 3 = 15$<br>$7 x 5 = 35$<br>Try out more examples to prove<br>your thinking.Image of finds are RUB by multiple (R).<br>They are to endow quark.<br>They are to endow quark.<br>The to endow quark.<br>They are to endow quark.<br>The to endow quark.<br>They are to endow quark.<br>They are to endow quark.<br>They are to endow qu |
|--|--|--|--|---|--|---|
| Known facts  | Recall and use x and ÷ fa  | Id use x and ÷ facts for the 3, 4 and 8 x tables   |  | Recall x and ÷ facts for x tables up to 12 x 12.  |  |   |
| Essential  | Review 2x, 5x and  | 10x Doub   | le 2 digit numbers   | 4x and 8x tables  |  | 10x bigger  |
| knowledge  | 4x table   |  | 3x table   | 3x, 6x and 12x  | tables   | Double larger numbers and<br>decimals   |
|  | 8 x table  |  | 6x table   | 3x and 9x ta  | ables  | 11x and 7x tables   |

| Year                                    | 5  |                              |   | 6  |   |  |
|---|--|------------------------------|---|--|---|--|
| Layers of                               | Basic to subject specific (Beck's Tiers):  |                              |   | Basic to subject specific (Beck's Tiers):  |   |  |
| vocabulary                              | lots of, groups of times, multiply, multiplication, multiplied by                            |                              |   | lots of, groups of times, multiply, multiplication, multiplied by multiple of, product |   |  |
| Tier 3                                  | multiple of, product once, twice, three times ten times times as                             |                              | once, twice, three times ten times times as (big, long, wide and so on)     |  |   |  |
| Vicebulary<br>Tier 3<br>Spronyms        | (big, long, wide and so on) repeated addition array row, column                              |                              | repeated addition array row, column double, halve share, share equally      |  |   |  |
| The 3<br>Bade words                     | double, halve share, share equally   |                              | factor, multiple, prime, composite  |  |   |  |
| Appendix 1a                             | factor, multiple, prime, composite   |                              |   |  |   |  |
| Beck's Tiers                            |  |                              |   |  |   |  |
| of                                      | Instructional vocabulary:  |                              |   | Instructional vocabulary:  |   |  |
| Vocabulary                              | carry on, continue, repeat what comes next? predict describe the                             |                              |   | carry on, continue, repeat what comes next? predict describe the pattern,              |   |  |
| Appendix                                | pattern, describe the rule   |                              |   | describe the rule  |   |  |
| 1b:                                     | find, find all, find different investigate   |                              | find, find all, find different investigate                                  |  |   |  |
| Vocabulary                              |  |                              |   |  |   |  |
| book                                    |  |                              |   |  |   |  |
| NC 2014                                 | Multiply numbers up  | to 4 digits by a 1 or 2      | digit number using a  | Multiply multi-digit numbers up to 4 digits by a 2 digit whole number using the        |   |  |
|   | formal written method, including long multiplication for 2 digit                             |                              |   | formal written method of long multiplication.  |   |  |
|   | numbers  |                              | Solve problems involving addition, subtraction, multiplication and division |  |   |  |
|   | Solve problems involving multiplication and division including using                         |                              | some provision and only subtraction, matuplication and anysion.             |  |   |  |
|   | knowledge of factors and multiples, squares and cubes  |                              |   |  |   |  |
|   | Solve problems involving addition subtraction multiplication and                             |                              |   |  |   |  |
|   | division and a combination of these including understanding the                              |                              |   |  |   |  |
|   | meaning of the equals sign<br>Solve problems involving multiplication and division including |                              |   |  |   |  |
|   |  |                              |   |  |   |  |
|   | scaling by simple fractions and problems involving simple rates                              |                              |   |  |   |  |
| Developing                              | Building tables  | Grid method                  | leading to compact  | Building tables  | If place value is secure, use grid            |  |
| Conceptual/                             |  | (if needed for<br>conceptual | 28  |  | 0.75 x 6                                      |  |
| Understanding                           | For example, apply   | understanding)               | <u>x 27</u>   | For example, apply tables knowledge to decimals using                                  |   |  |
| - · · · · · · · · · · · · · · · · · · · | multiples of 10, 100 and   | 28 x 2/                      | 196<br>₅  | missing jumps  | $0.7 \times 6 = 4.2$<br>$0.05 \times 6 = 0.3$ |  |
|   | 1000 using counting  | 20 0                         | <u>560</u>  |  | $0.75 \times 6 = 4.5$                         |  |
|   | backwards and with   | Addition to be done          | <u>756</u>  | If $2 \times 3 = 6$ then $0.2 \times 3 = 0.6$ and $0.02 \times 3 = 0.06$               | Make explicit links between decimals          |  |
|   | missing jumps  | mentally or across           | <sup>1</sup><br>Extend to HTU x TU or                                       | Long multiplication  | and money                                     |  |
|   | Using known facts  | addition                     | ThHTU x TU as appropriate   | Use expanded method first if needed to build conceptual                                |   |  |
|   | If 2 x 3 = 6 then 2000 x 3   |                              | Representing problems   | understanding  | x 0.7 0.05                                    |  |
|   | = 6000 and   | Expanded                     | 40 cupcakes cost £3.60, how   | 5172   | 6   |  |
|   | 200 x 30 - 0000  | 28                           | much do 20 cupcakes cost?   | <u>x 27</u>  |   |  |
|   | Place value materials  | $\frac{x \ 27}{56}$          | cost? How much do 10  | 36204<br>1 51  |   |  |
|   | calculations   | 140 (7 x20)                  | cupcakes cost?  | <u>103440</u>  | Representing problems                         |  |
|   |  | 160 (20x8)<br>400 (20x20)    |   | 139644   | 600. She says "I can do this without a        |  |
|   |  | 756                          |   |  | written method." Write down the               |  |
|   |  |                              |   |  | mentar steps you trillik Ainy could do.       |  |
|   |  |                              |   |  |   |  |
|   |  |                              |   |  |   |  |

|             | Short multiplication<br>Use expanded method<br>first if needed to build<br>conceptual<br>understanding<br>4346<br><u>x 8</u><br><u>34768</u><br>234 |  |   |  | presented so the same as 2 manufactors<br>Demmany costs E1.35<br>Terminologies and presented as a constrained of the same presented of t |
|-------------|---|--|---|--|--|
| Known facts | Know and use the vocabulary of prime numbers, prime factors and   |  | Identify common factors, common multiples and prime numbers |  |  |
|             | composite (non-prime) numbers   |  |   |  |  |
|             | Recall prime numbers up to 19   |  |   |  |  |
|             | Recognise and use square and cube numbers and the notation for  |  |   |  |  |
|             | squared ( <sup>2</sup> ) and cubed ( <sup>3</sup> )   |  |   |  |  |
| Essential   | 4x and 8x tables  |  | 100, 1000   | Multiplication facts up to 12 x 12                       | Partition to multiply  |
| knowledge   |   |  | times bigger  |  | mentally   |
|             | 3x, 6x and 12x tables; 3x and 9x tables<br>11x and 7x tables  |  | 10, 100, 1000   | Apply place value to derive multiplication facts, e.g. 3 | Double larger numbers  |
|             |   |  | times smaller   | x 4 = 12 so 3 x 0.4 = 1.2                                | and decimals   |
|             |   |  | Double larger   |  |  |
|             |   |  | numbers and   |  |  |
|             |   |  | decimals  |  |  |